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Vanishing theorems in the cohomology ring of the moduli space of parabolic vector bundles

Let Σ be a compact connected oriented 2-manifold of genus $g \ge 2$, and let p be a point on Σ . We define a space $S_g(t)$ consisting of certain irreducible representations of the fundamental group of $\Sigma \setminus p$, modulo conjugation by SU(n). This space has interpretations in algebraic geometry, gauge theory and topological quantum field theory; in particular if Σ has a Kahler structure then $S_g(t)$ is the moduli space of parabolic vector bundles of rank n over Σ .

For n = 2, Weitsman considered a tautological line bundle on $S_g(t)$, and proved that the $(2g)^{th}$ power of its first Chern class vanishes, as conjectured by Newstead. In this talk I will present his proof and then outline my extension of his work to SU(n) and SO(2n + 1).